



# Organometálicos 2

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Aula 11 -Organometálicos

Simetria  $T_d$



12/06/2024

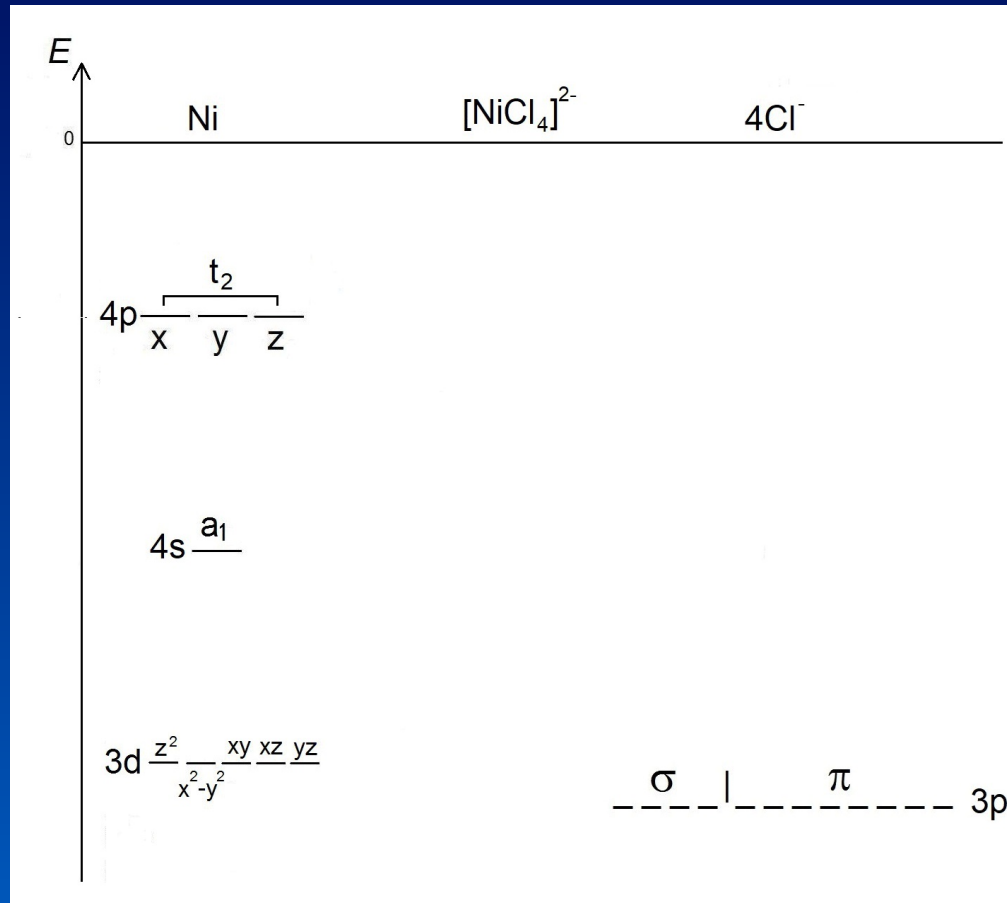
# $[\text{NiCl}_4]^{2-} - \text{T}_d$

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| $\text{T}_d$ | E | $8\text{C}_3$ | $3\text{C}_2$ | $6\text{S}_4$ | $6\sigma_d$ |
|--------------|---|---------------|---------------|---------------|-------------|
| $\text{A}_1$ | 1 | 1             | 1             | 1             | 1           |
| $\text{A}_2$ | 1 | 1             | 1             | -1            | -1          |
| E            | 2 | -1            | 2             | 0             | 0           |
| $\text{T}_1$ | 3 | 0             | -1            | 1             | -1          |
| $\text{T}_2$ | 3 | 0             | -1            | -1            | 1           |

# $[\text{NiCl}_4]^{2-} - T_d$

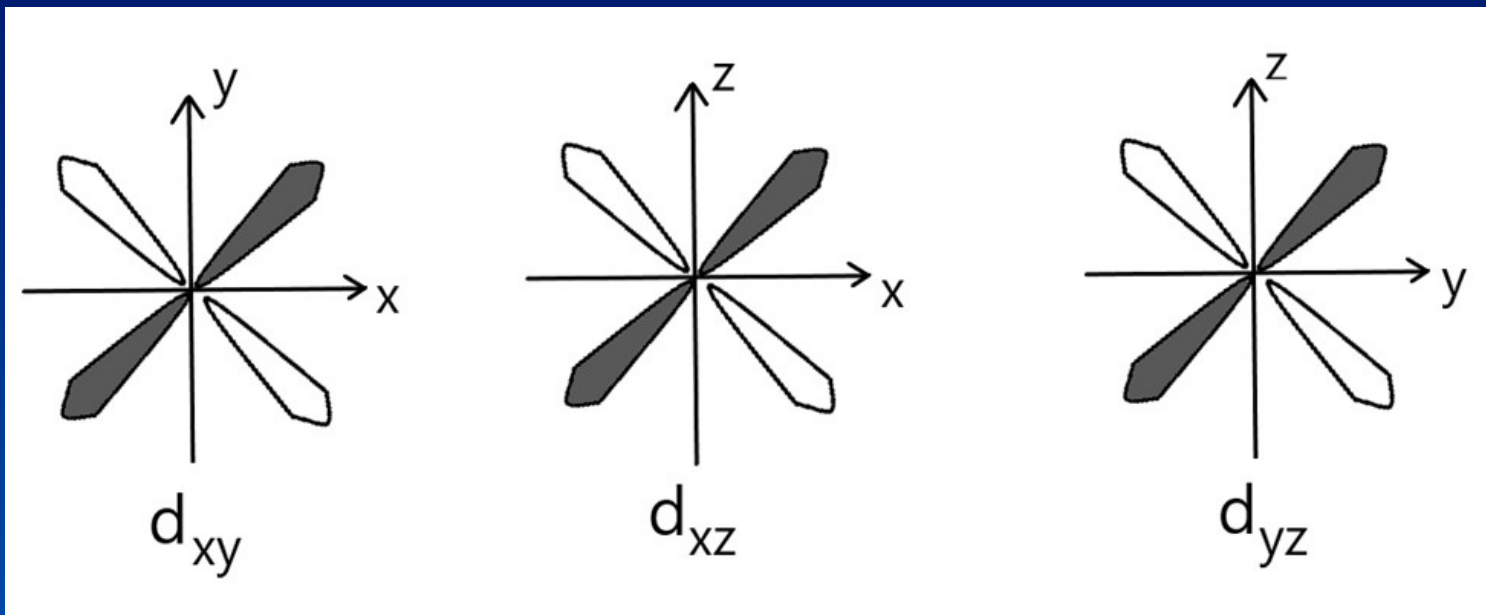
## Diagrama de energia dos orbitais moleculares



Aproveitando os resultados do metano,  $T_d$

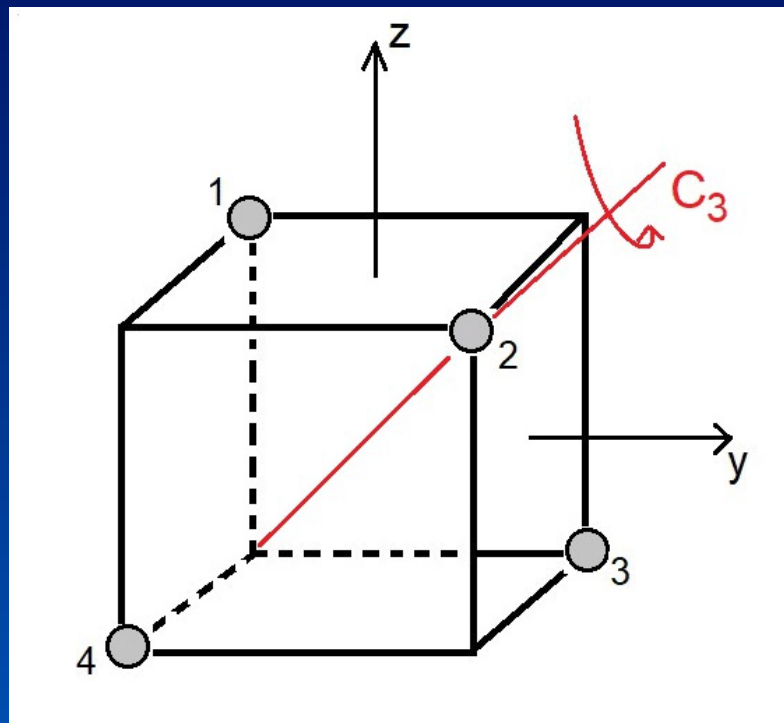
# $[\text{NiCl}_4]^{2-} - \text{T}_d$

Classificando os orbitais 3d (xy,xz,yz) do Ni - INSEPARÁVEIS



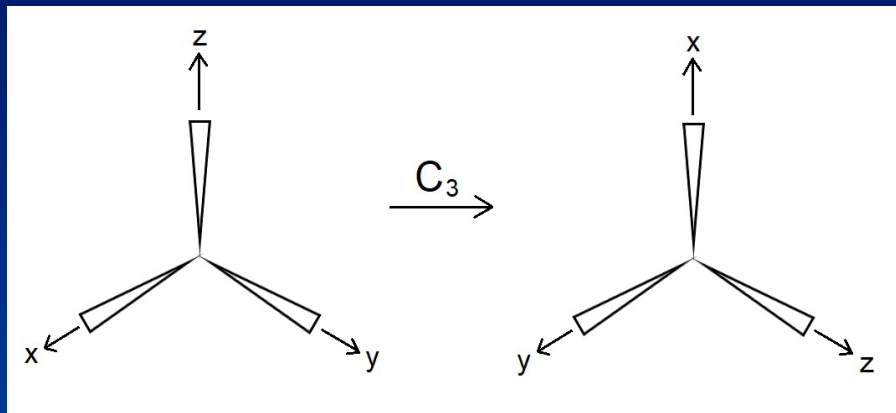
# $[\text{NiCl}_4]^{2-} - T_d$

Classificando os orbitais 3d (xy,xz,yz) do Ni - INSEPARÁVEIS



# $[\text{NiCl}_4]^{2-} - T_d$

Classificando os orbitais 3d (xy,xz,yz) do Ni - INSEPARÁVEIS



$$\begin{aligned} x &-C_3 \rightarrow y \\ y &-C_3 \rightarrow z \\ z &-C_3 \rightarrow x \end{aligned}$$

# $[\text{NiCl}_4]^{2-} - \text{T}_d$

Classificando os orbitais 3d (xy,xz,yz) do Ni - INSEPARÁVEIS

$$x - C_3 \rightarrow z$$

$$y - C_3 \rightarrow x$$

$$z - C_3 \rightarrow y$$

$$d_{xy} - C_3 \rightarrow d_{zx} = d_{xz}$$

$$d_{xz} - C_3 \rightarrow d_{zy} = d_{yz}$$

$$d_{yz} - C_3 \rightarrow d_{xy}$$

$$\begin{array}{c}
 \\
 d_{xy} \\
 d_{xz} \\
 d_{yz}
 \end{array}
 \begin{array}{ccc}
 d_{xy} & d_{xz} & d_{yz} \\
 1 & 0 & 0 \\
 0 & 1 & 0 \\
 0 & 0 & 1
 \end{array}
 \xrightarrow{C_3}
 \begin{array}{c}
 \\
 d_{xy} \\
 d_{xz} \\
 d_{yz}
 \end{array}
 \begin{array}{ccc}
 d_{xy} & d_{xz} & d_{yz} \\
 0 & 1 & 0 \\
 0 & 0 & 1 \\
 1 & 0 & 0
 \end{array}$$

$$\chi = 0$$

# $[\text{NiCl}_4]^{2-} - \text{T}_d$

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Classificando os orbitais 3d (xy,xz,yz) do Ni -INSEPARÁVEIS

| $\text{T}_d$ | E | $8\text{C}_3$ | $3\text{C}_2$ | $6\text{S}_4$ | $6\sigma_d$ |
|--------------|---|---------------|---------------|---------------|-------------|
| $\text{A}_1$ | 1 | 1             | 1             | 1             | 1           |
| $\text{A}_2$ | 1 | 1             | 1             | -1            | -1          |
| E            | 2 | -1            | 2             | 0             | 0           |
| $\text{T}_1$ | 3 | 0             | -1            | 1             | -1          |
| $\text{T}_2$ | 3 | 0             | -1            | -1            | 1           |

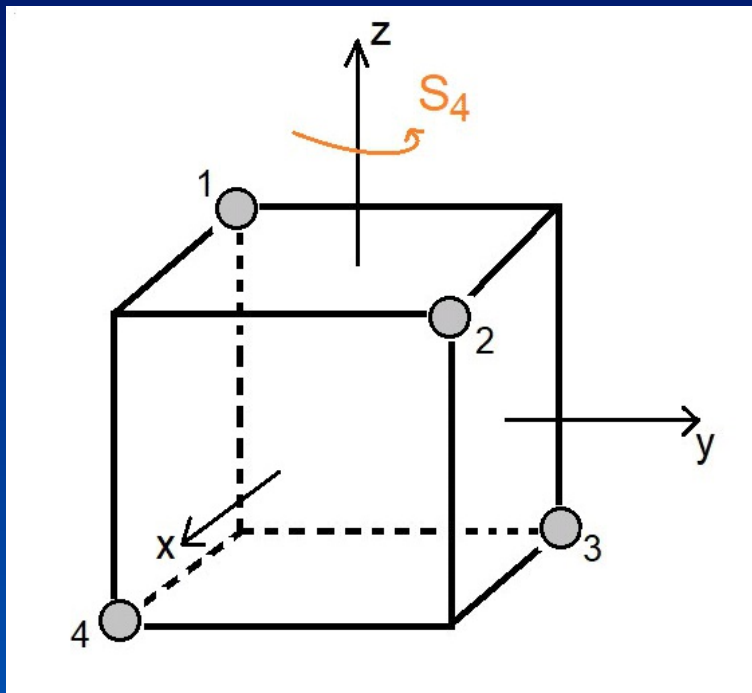
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|                         |   |   |
|-------------------------|---|---|
| $(\text{d}_{xy,xz,yz})$ | 3 | 0 |
|-------------------------|---|---|



# $[\text{NiCl}_4]^{2-} - T_d$

Classificando os orbitais 3d (xy,xz,yz) do Ni - INSEPARÁVEIS



$$\begin{aligned} x &- {}^{(z)}S_4 \rightarrow y \\ y &- {}^{(z)}S_4 \rightarrow -x \\ z &- {}^{(z)}S_4 \rightarrow -z \end{aligned}$$

# $[\text{NiCl}_4]^{2-} - T_d$

Classificando os orbitais 3d (xy,xz,yz) do Ni - INSEPARÁVEIS

$$\begin{aligned} x &- {}^{(z)}S_4 \rightarrow y \\ y &- {}^{(z)}S_4 \rightarrow -x \\ z &- {}^{(z)}S_4 \rightarrow -z \end{aligned}$$

$$\begin{aligned} d_{xy} &- {}^{(z)}S_4 \rightarrow d_{y(-x)} = -d_{xy} \\ d_{xz} &- {}^{(z)}S_4 \rightarrow d_{y(-z)} = -d_{yz} \\ d_{yz} &- {}^{(z)}S_4 \rightarrow d_{(-x)(-z)} = d_{xz} \end{aligned}$$

$$\begin{array}{ccc} & d_{xy} & d_{xz} & d_{yz} \\ \begin{array}{c} d_{xy} \\ d_{xz} \\ d_{yz} \end{array} & \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix} & \xrightarrow{{}^{(z)}S_4} & \begin{array}{ccc} d_{xy} & d_{xz} & d_{yz} \\ \begin{pmatrix} -1 & 0 & 0 \\ 0 & 0 & -1 \\ 0 & 1 & 0 \end{pmatrix} \end{array} \end{array}$$

$$\chi = -1$$

# $[\text{NiCl}_4]^{2-} - T_d$

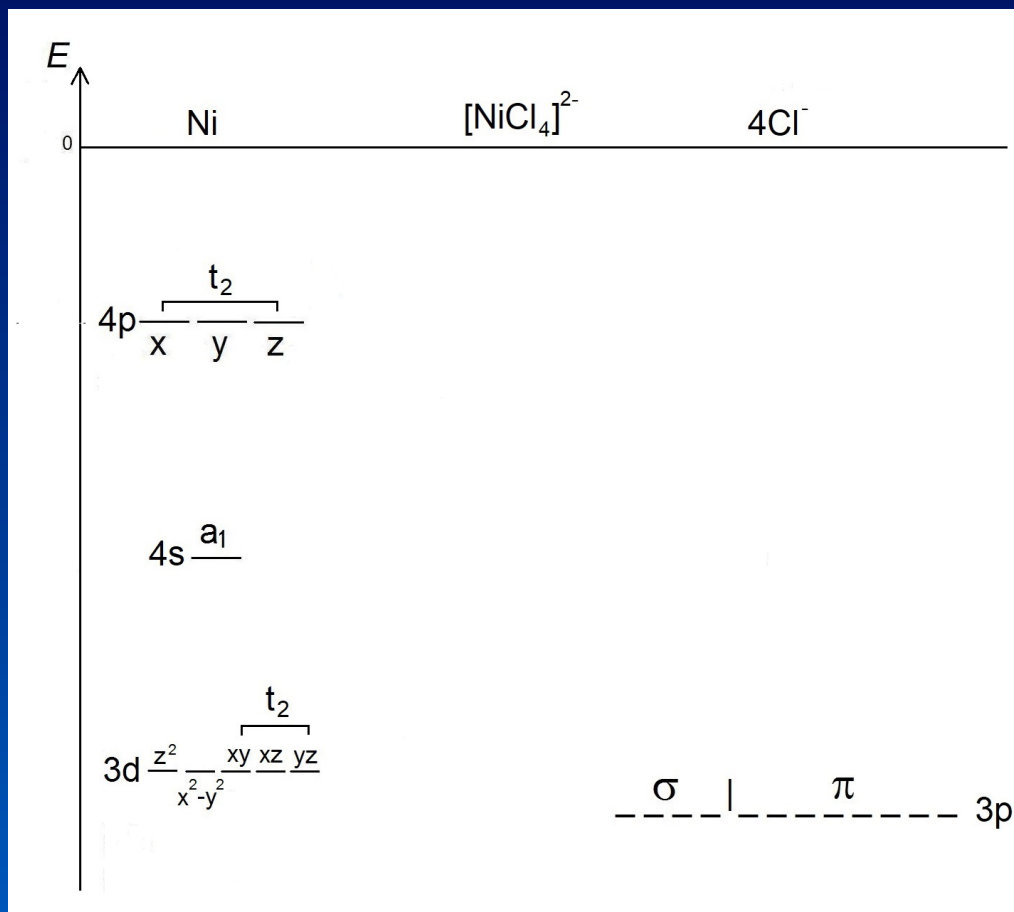
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Classificando os orbitais 3d (xy,xz,yz) do Ni -INSEPARÁVEIS

| $T_d$            | E | $8C_3$ | $3C_2$ | $6S_4$ | $6\sigma_d$ |
|------------------|---|--------|--------|--------|-------------|
| $A_1$            | 1 | 1      | 1      | 1      | 1           |
| $A_2$            | 1 | 1      | 1      | -1     | -1          |
| E                | 2 | -1     | 2      | 0      | 0           |
| $T_1$            | 3 | 0      | -1     | 1      | -1          |
| $T_2$            | 3 | 0      | -1     | -1     | 1           |
| <hr/>            |   |        |        |        |             |
| $(d_{xy,xz,yz})$ | 3 | 0      |        | -1     | $T_2$       |

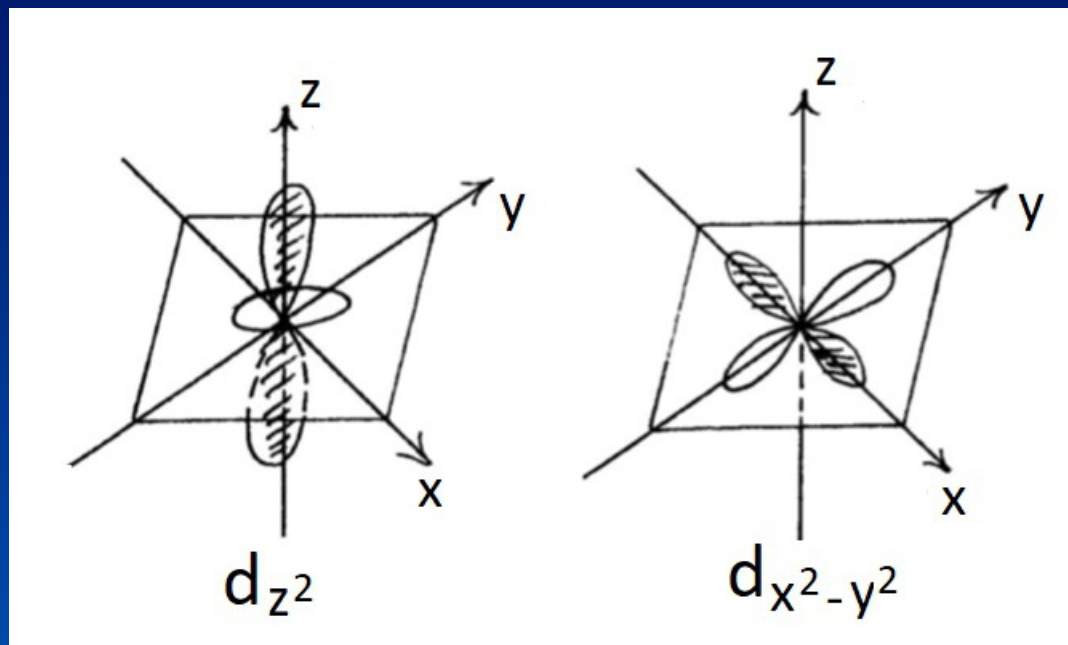
# $[\text{NiCl}_4]^{2-} - \text{T}_d$

Diagrama de energia dos orbitais moleculares



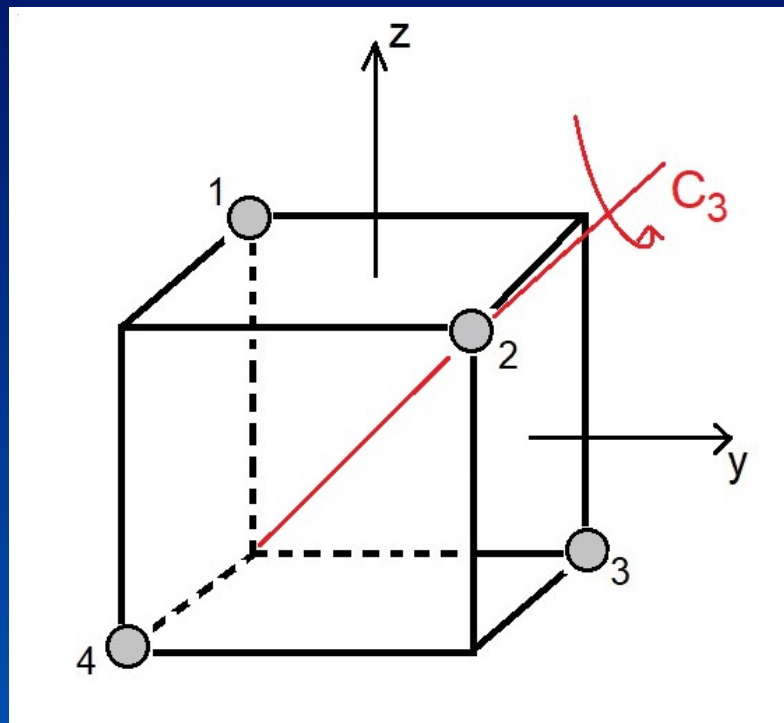
# $[\text{NiCl}_4]^{2-} - T_d$

Classificando os orbitais 3d ( $z^2, x^2-y^2$ ) do Ni - INSEPARÁVEIS



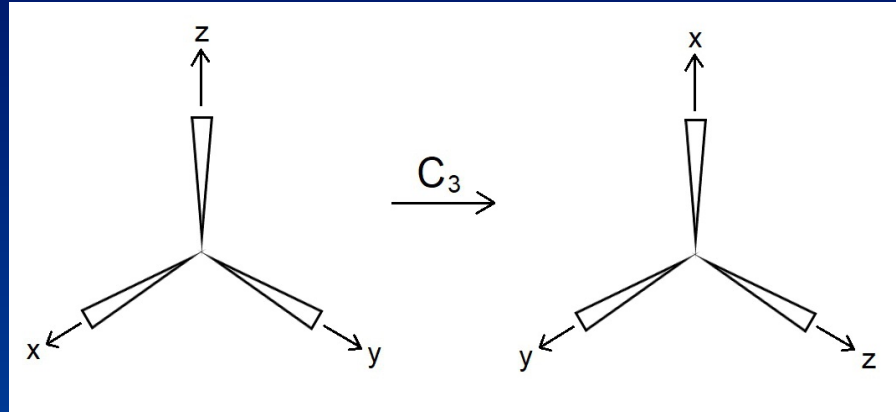
# $[\text{NiCl}_4]^{2-} - T_d$

Classificando os orbitais 3d ( $z^2, x^2-y^2$ ) do Ni - INSEPARÁVEIS



# $[\text{NiCl}_4]^{2-} - T_d$

Classificando os orbitais 3d ( $z^2, x^2-y^2$ ) do Ni - INSEPARÁVEIS



$$\begin{array}{lcl} x & \xrightarrow{C_3} & y \\ y & \xrightarrow{C_3} & z \\ z & \xrightarrow{C_3} & x \end{array}$$

# $[\text{NiCl}_4]^{2-} - \text{T}_d$

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Classificando os orbitais 3d ( $z^2, x^2-y^2$ ) do Ni - INSEPARÁVEIS

$$x - C_3 \rightarrow y$$

$$y - C_3 \rightarrow z$$

$$z - C_3 \rightarrow x$$

$$d_{z^2} \quad C_3 \rightarrow d_{x^2}$$

$$d_{x^2-y^2} \quad C_3 \rightarrow d_{y^2-z^2}$$

Na verdade, a expressão do orbital  $d_{z^2}$  é mais complexa:

$$d_{z^2} = (1/\sqrt{3})(2z^2 - x^2 - y^2) \quad C_3 \rightarrow d_{x^2} = (1/\sqrt{3})(2x^2 - y^2 - z^2)$$

$$d_{x^2-y^2} = x^2 - y^2 \quad C_3 \rightarrow d_{y^2-z^2} = y^2 - z^2$$



# $[\text{NiCl}_4]^{2-} - T_d$

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Classificando os orbitais 3d ( $z^2, x^2-y^2$ ) do Ni - INSEPARÁVEIS

Pode-se mostrar que os novos orbitais  $d_{x^2}$  e  $d_{y^2-z^2}$  são uma combinação linear dos orbitais  $d_{z^2}$  e  $d_{x^2-y^2}$ .

$$d_{x^2} = (1/\sqrt{3})(2x^2 - y^2 - z^2) = C_{11} (1/\sqrt{3})(2z^2 - x^2 - y^2) + C_{12}(x^2 - y^2)$$

$$d_{y^2-z^2} = y^2 - z^2 = C_{21} (1/\sqrt{3})(2z^2 - x^2 - y^2) + C_{22}(x^2 - y^2)$$

Colecionando-se os termos de  $z^2$  da primeira equação, obtém-se o valor de  $C_{11}$ :

$$-(1/\sqrt{3}) = C_{11} (1/\sqrt{3}) \times 2$$

$$C_{11} = -1/2$$

# $[\text{NiCl}_4]^{2-} - T_d$

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Classificando os orbitais 3d ( $z^2, x^2-y^2$ ) do Ni - INSEPARÁVEIS

$$d_{x^2} = (1/\sqrt{3})(2x^2 - y^2 - z^2) = C_{11} (1/\sqrt{3})(2z^2 - x^2 - y^2) + C_{12}(x^2 - y^2)$$

$$d_{y^2-z^2} = y^2 - z^2 = C_{21} (1/\sqrt{3})(2z^2 - x^2 - y^2) + C_{22}(x^2 - y^2)$$

Colecionando-se os termos de  $y^2$  da primeira equação, obtém-se o valor de  $C_{12}$ :

$$-(1/\sqrt{3}) = -C_{11} (1/\sqrt{3}) - C_{12}$$

$$-(1/\sqrt{3}) = -(-1/2)(1/\sqrt{3}) - C_{12}$$

$$C_{12} = (1/\sqrt{3}) + (1/2)(1/\sqrt{3}) = (\sqrt{3})/2$$

# $[\text{NiCl}_4]^{2-} - T_d$

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Classificando os orbitais 3d ( $z^2, x^2-y^2$ ) do Ni - INSEPARÁVEIS

$$d_{x^2} = (1/\sqrt{3})(2x^2 - y^2 - z^2) = C_{11} (1/\sqrt{3})(2z^2 - x^2 - y^2) + C_{12}(x^2 - y^2)$$

$$d_{y^2-z^2} = y^2 - z^2 = C_{21} (1/\sqrt{3})(2z^2 - x^2 - y^2) + C_{22}(x^2 - y^2)$$

Colecionando-se os termos de  $z^2$  da segunda equação, obtém-se o valor de  $C_{21}$ :

$$-1 = C_{21} (2/\sqrt{3})$$

$$C_{21} = -(\sqrt{3})/2$$

# $[\text{NiCl}_4]^{2-} - T_d$

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Classificando os orbitais 3d ( $z^2, x^2-y^2$ ) do Ni - INSEPARÁVEIS

$$d_{x^2} = (1/\sqrt{3})(2x^2 - y^2 - z^2) = C_{11} (1/\sqrt{3})(2z^2 - x^2 - y^2) + C_{12}(x^2 - y^2)$$

$$d_{y^2-z^2} = y^2 - z^2 = C_{21} (1/\sqrt{3})(2z^2 - x^2 - y^2) + C_{22}(x^2 - y^2)$$

Colecionando-se os termos de  $y^2$  da segunda equação, obtém-se o valor de  $C_{22}$ :

$$\begin{aligned} 1 &= -C_{21} (1/\sqrt{3}) - C_{22} \\ 1 &= (\sqrt{3}/2)(1/\sqrt{3}) - C_{22} \\ C_{22} &= -1 + 1/2 = \mathbf{-1/2} \end{aligned}$$

# $[\text{NiCl}_4]^{2-} - T_d$

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Classificando os orbitais 3d ( $z^2, x^2-y^2$ ) do Ni - INSEPARÁVEIS

$$\begin{array}{cc}
 & \begin{array}{cc} d_{z^2} & d_{x^2-y^2} \end{array} \\
 \begin{array}{c} d_{z^2} \\ d_{x^2-y^2} \end{array} & \begin{array}{cc} 1 & 0 \\ 0 & 1 \end{array}
 \end{array}
 \xrightarrow{C_3}
 \begin{array}{cc}
 & \begin{array}{cc} d_{z^2} & d_{x^2-y^2} \end{array} \\
 \begin{array}{c} d_{z^2} \\ d_{x^2-y^2} \end{array} & \begin{array}{cc} -1/2 & (\sqrt{3})/2 \\ -(\sqrt{3})/2 & -1/2 \end{array}
 \end{array}$$

$$\chi = -1$$

# $[\text{NiCl}_4]^{2-} - \text{T}_d$

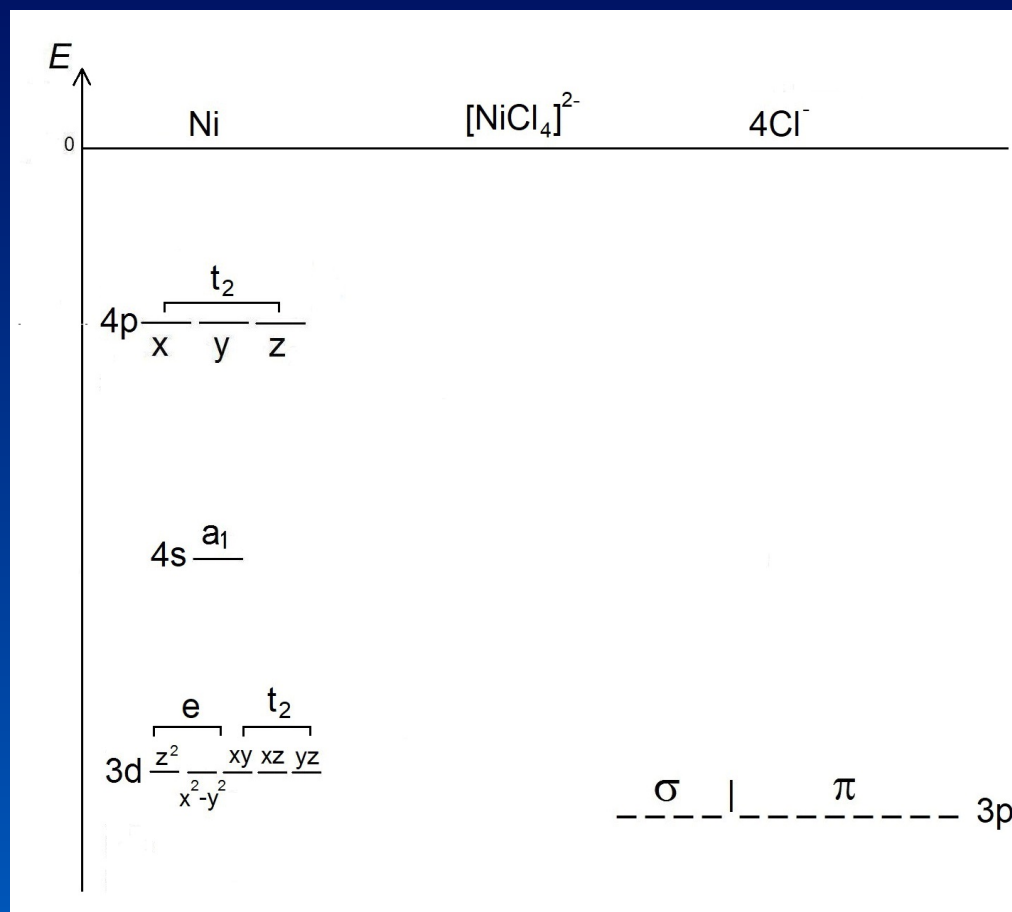
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Classificando os orbitais 3d ( $z^2, x^2-y^2$ ) do Ni -INSEPARÁVEIS

| $\text{T}_d$                | E | $8\text{C}_3$ | $3\text{C}_2$ | $6\text{S}_4$ | $6\sigma_d$ |
|-----------------------------|---|---------------|---------------|---------------|-------------|
| $\text{A}_1$                | 1 | 1             | 1             | 1             | 1           |
| $\text{A}_2$                | 1 | 1             | 1             | -1            | -1          |
| E                           | 2 | -1            | 2             | 0             | 0           |
| $\text{T}_1$                | 3 | 0             | -1            | 1             | -1          |
| $\text{T}_2$                | 3 | 0             | -1            | -1            | 1           |
| <hr/>                       |   |               |               |               |             |
| $(\text{d}_{z^2, x^2-y^2})$ | 2 | -1            |               |               | E           |

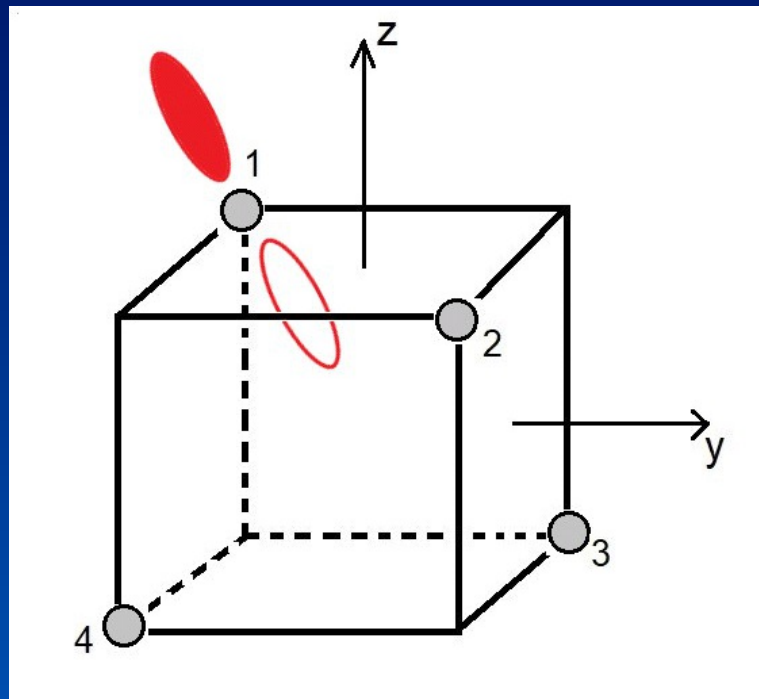
# $[\text{NiCl}_4]^{2-} - \text{T}_d$

## Diagrama de energia dos orbitais moleculares



# $[\text{NiCl}_4]^{2-} - T_d$

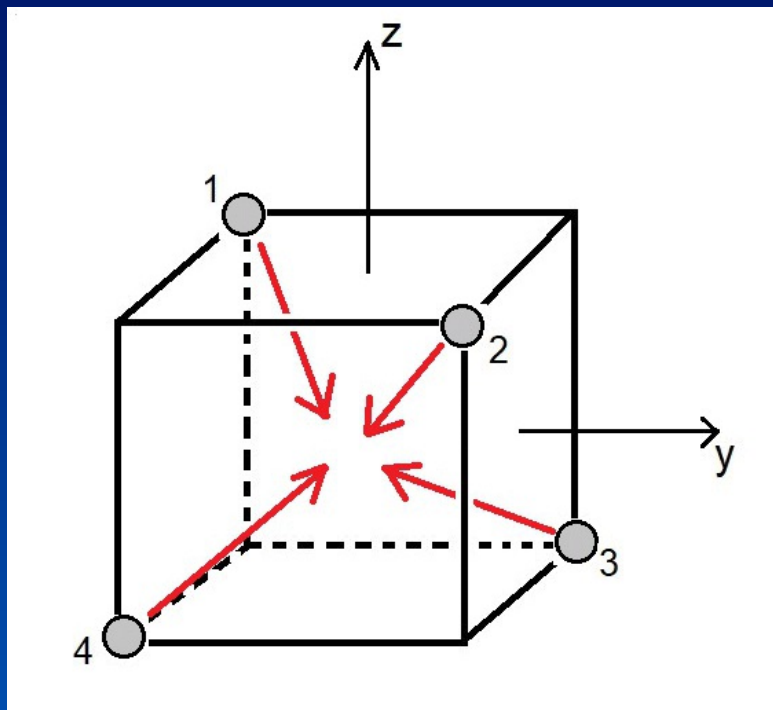
Classificando os orbitais  $p\sigma$  dos ligantes cloreto -INSEPARÁVEIS





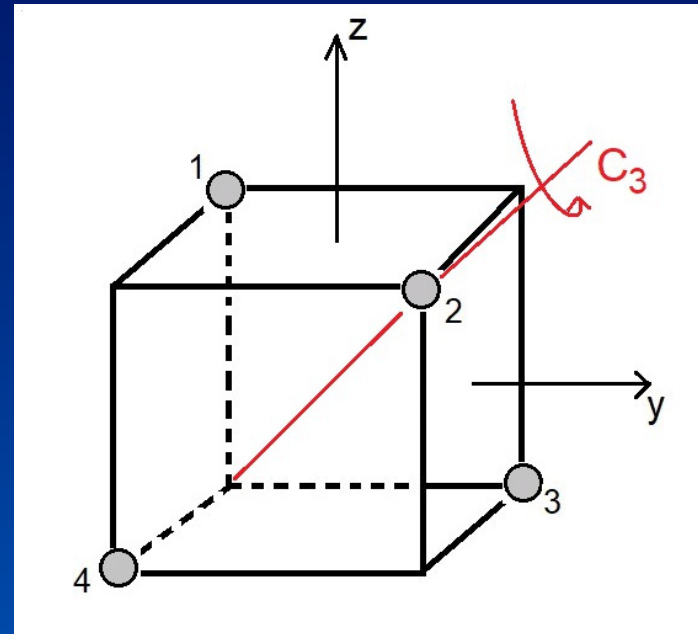
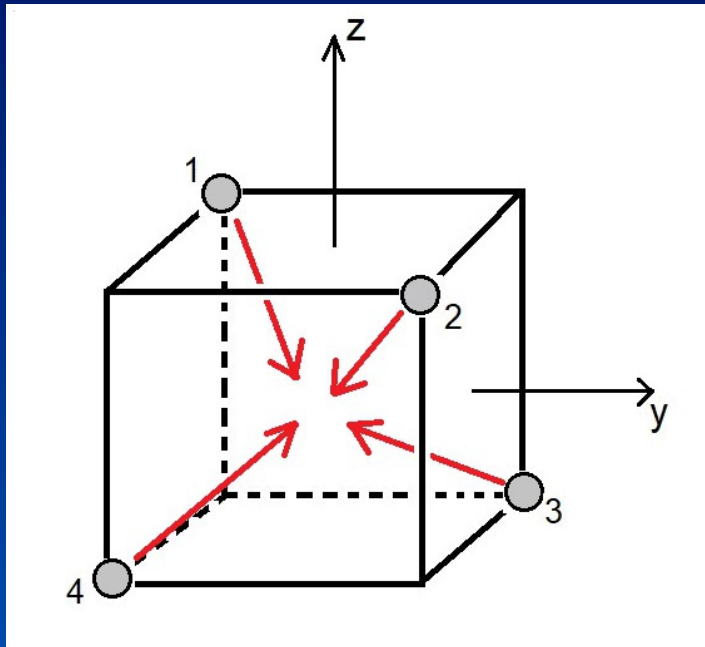
# $[\text{NiCl}_4]^{2-} - T_d$

Classificando os orbitais  $p\sigma$  dos ligantes cloreto -INSEPARÁVEIS



# $[\text{NiCl}_4]^{2-} - T_d$

Classificando os orbitais  $p\sigma$  dos ligantes cloreto -INSEPARÁVEIS



# $[\text{NiCl}_4]^{2-} - \text{T}_d$

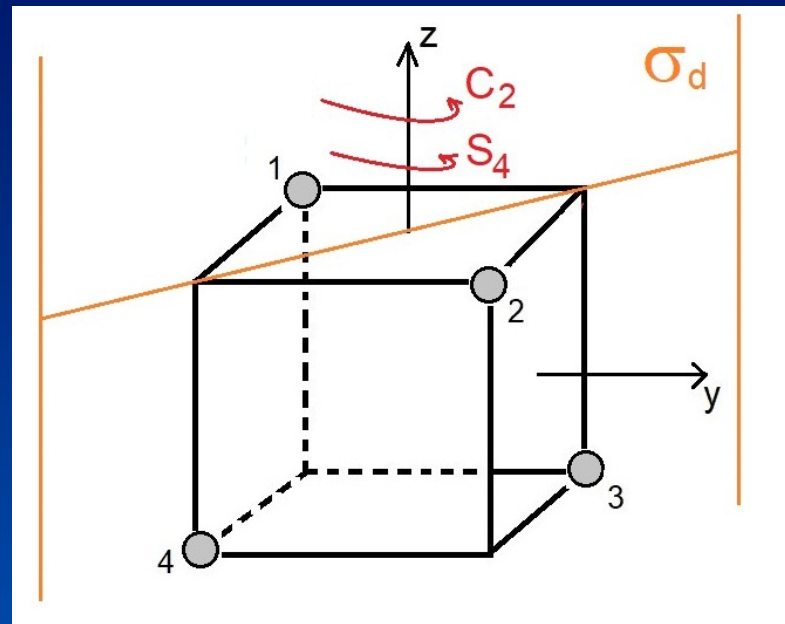
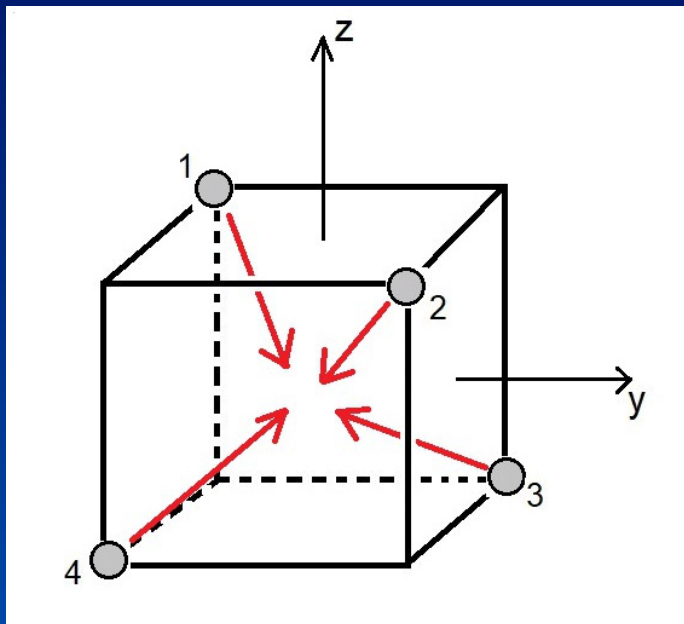
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Classificando os orbitais  $p\sigma$  dos ligantes cloreto -INSEPARÁVEIS

| $\text{T}_d$       | E | $8\text{C}_3$ | $3\text{C}_2$ | $6\text{S}_4$ | $6\sigma_d$ |
|--------------------|---|---------------|---------------|---------------|-------------|
| $\text{A}_1$       | 1 | 1             | 1             | 1             | 1           |
| $\text{A}_2$       | 1 | 1             | 1             | -1            | -1          |
| E                  | 2 | -1            | 2             | 0             | 0           |
| $\text{T}_1$       | 3 | 0             | -1            | 1             | -1          |
| $\text{T}_2$       | 3 | 0             | -1            | -1            | 1           |
| <hr/>              |   |               |               |               |             |
| $p\sigma(1,2,3,4)$ | 4 | 1             |               |               |             |

# $[\text{NiCl}_4]^{2-} - T_d$

Classificando os orbitais  $p\sigma$  dos ligantes cloreto -INSEPARÁVEIS



# $[\text{NiCl}_4]^{2-} - T_d$

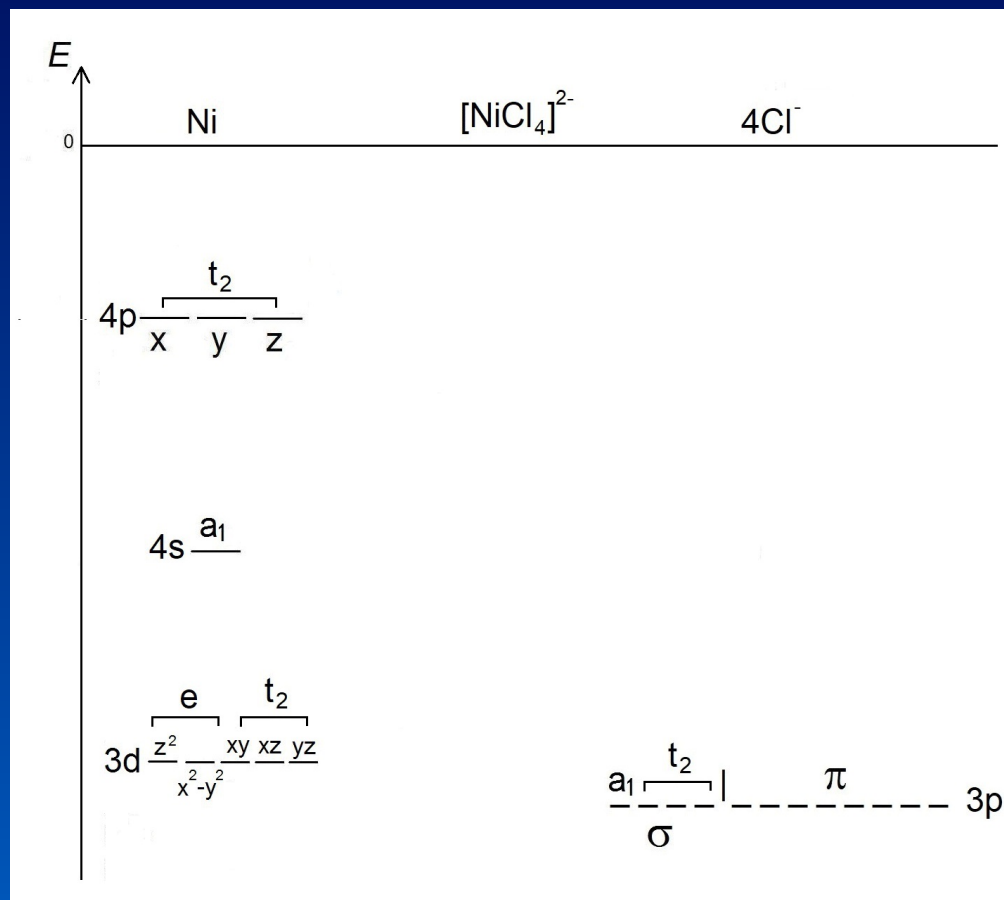
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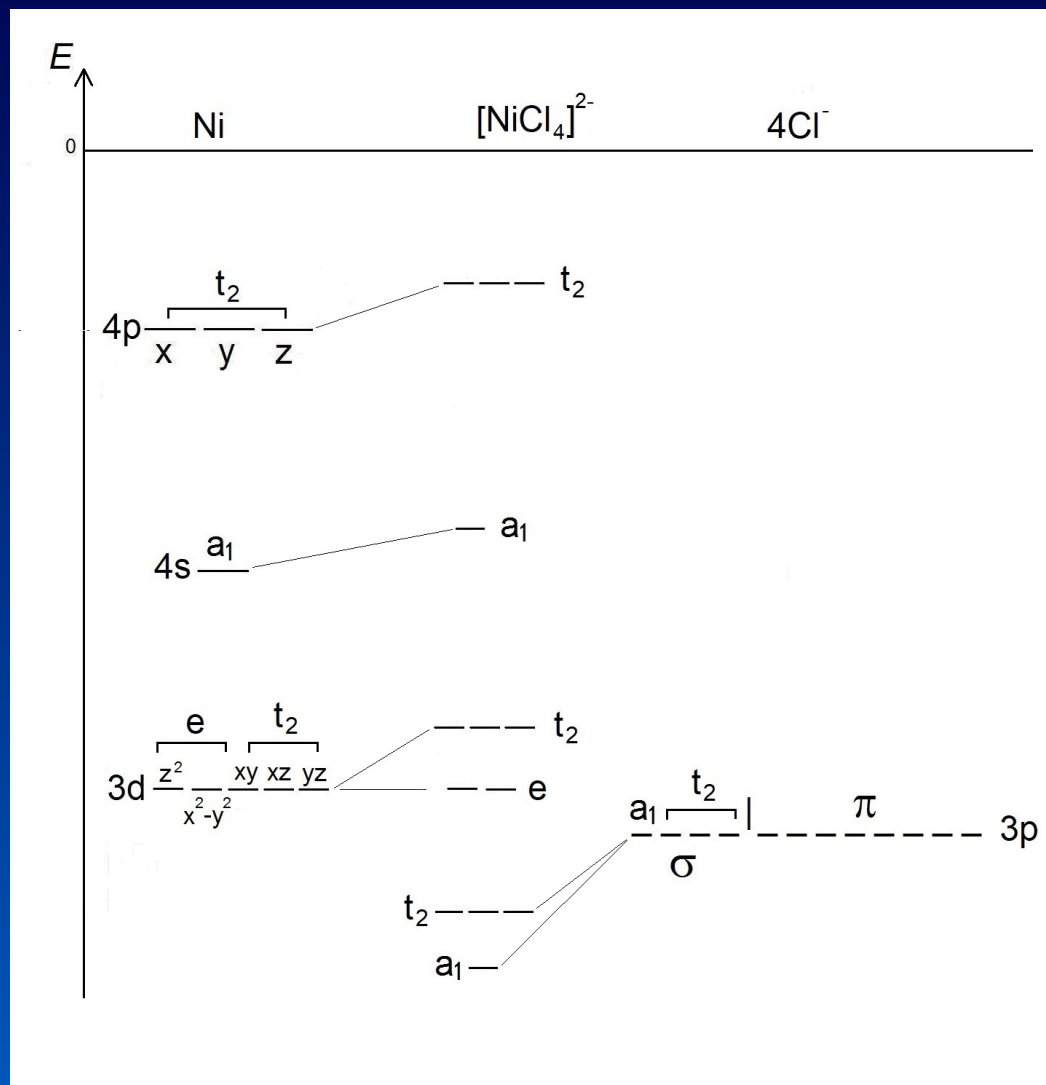
Classificando os orbitais  $p\sigma$  dos ligantes cloreto -INSEPARÁVEIS

| $T_d$              | E | $8C_3$ | $3C_2$ | $6S_4$ | $6\sigma_d$ |             |
|--------------------|---|--------|--------|--------|-------------|-------------|
| $A_1$              | 1 | 1      | 1      | 1      | 1           |             |
| $A_2$              | 1 | 1      | 1      | -1     | -1          |             |
| E                  | 2 | -1     | 2      | 0      | 0           |             |
| $T_1$              | 3 | 0      | -1     | 1      | -1          |             |
| $T_2$              | 3 | 0      | -1     | -1     | 1           |             |
| <hr/>              |   |        |        |        |             |             |
| $p\sigma(1,2,3,4)$ | 4 | 1      | 0      | 0      | 2           | $A_1 + T_2$ |

# $[\text{NiCl}_4]^{2-} - \text{T}_d$

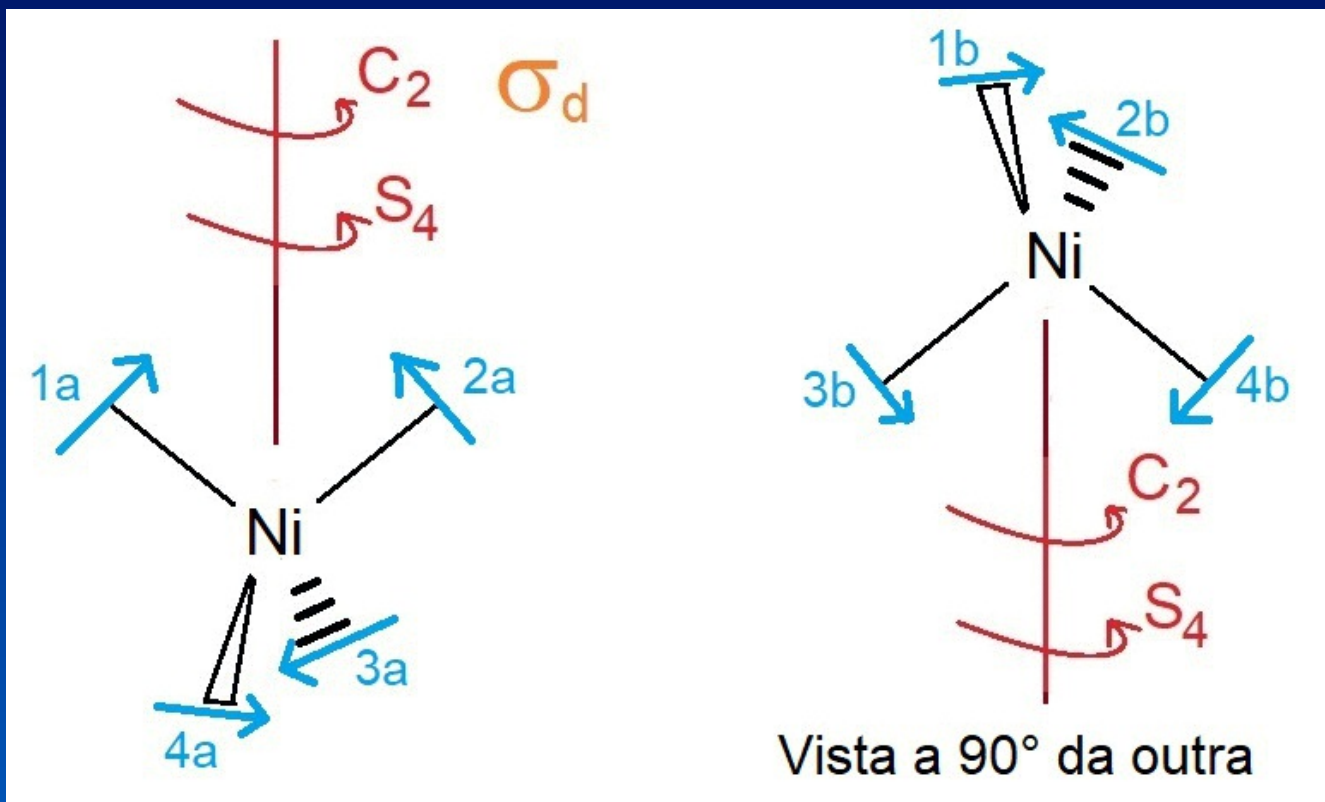
Diagrama de energia dos orbitais moleculares





# $[\text{NiCl}_4]^{2-} - T_d$

Classificando os orbitais  $p\pi$  dos ligantes cloreto -INSEPARÁVEIS





# $[\text{NiCl}_4]^{2-} - \text{T}_d$

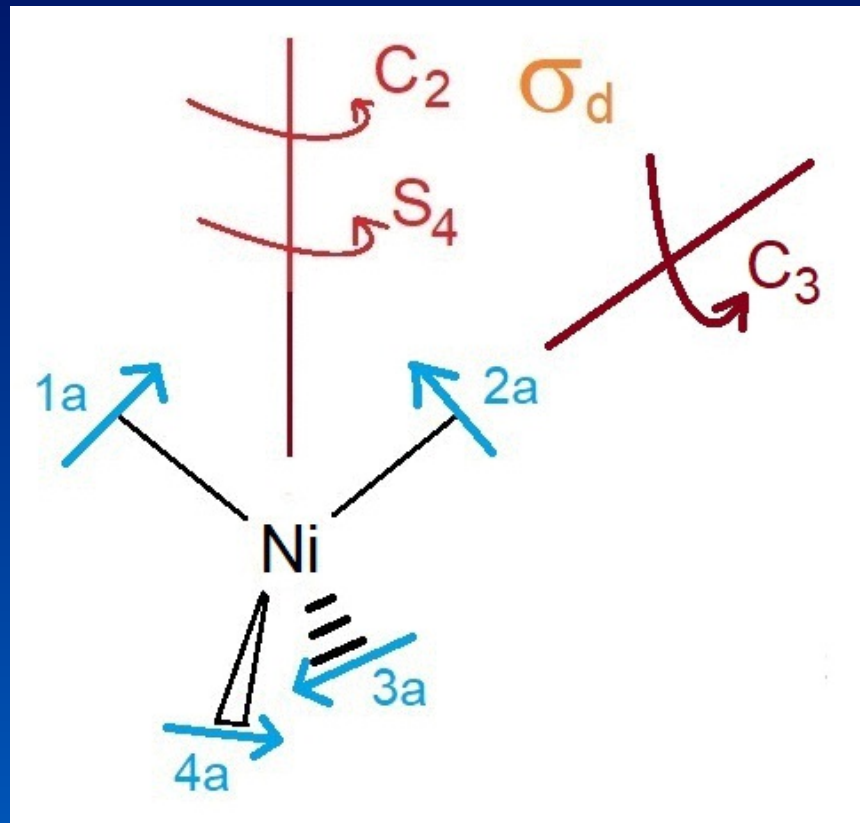
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Classificando os orbitais  $p\pi$  dos ligantes cloreto -INSEPARÁVEIS

| $\text{T}_d$           | E | $8\text{C}_3$ | $3\text{C}_2$ | $6\text{S}_4$ | $6\sigma_d$ |
|------------------------|---|---------------|---------------|---------------|-------------|
| $\text{A}_1$           | 1 | 1             | 1             | 1             | 1           |
| $\text{A}_2$           | 1 | 1             | 1             | -1            | -1          |
| E                      | 2 | -1            | 2             | 0             | 0           |
| $\text{T}_1$           | 3 | 0             | -1            | 1             | -1          |
| $\text{T}_2$           | 3 | 0             | -1            | -1            | 1           |
| <hr/>                  |   |               |               |               |             |
| $p\pi(1 \text{ a } 8)$ | 8 |               | 0             | 0             | 0           |

# $[\text{NiCl}_4]^{2-} - T_d$

Classificando os orbitais  $p\pi$  dos ligantes cloreto -INSEPARÁVEIS

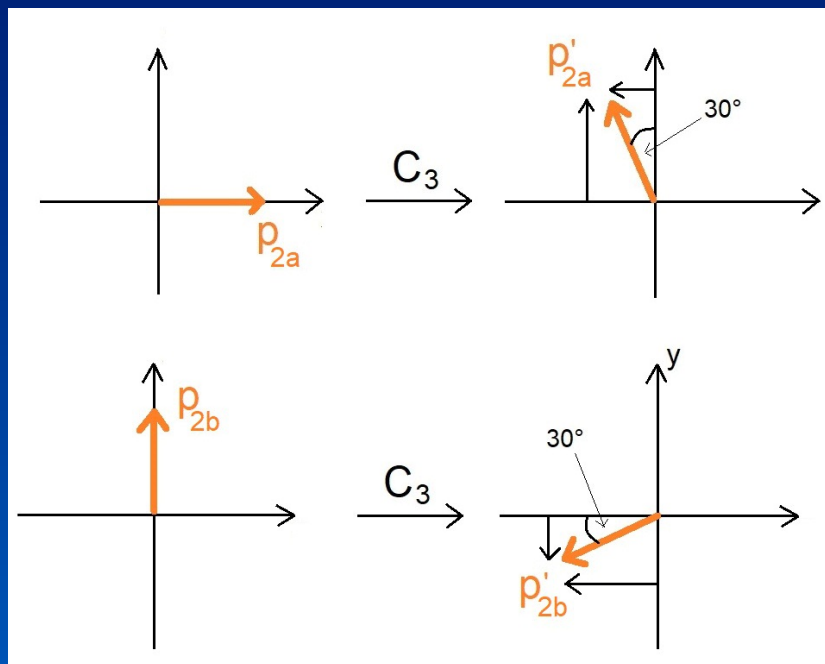


# $[\text{NiCl}_4]^{2-} - \text{T}_d$

Os orbitais  $p_{2a}$  e  $p_{2b}$  do Cl são **INSEPARÁVEIS**

$$p_{2a}' = -p_{2a} \sin 30^\circ + p_{2b} \cos 30^\circ = (-1/2)p_{2a} + (\sqrt{3}/2)p_{2b}$$

$$p_{2b}' = -p_{2a} \cos 30^\circ - p_{2b} \sin 30^\circ = (-\sqrt{3}/2)p_{2a} + (-1/2)p_{2b}$$



# $[\text{NiCl}_4]^{2-} - \text{T}_d$

Os orbitais  $p_{2a}$  e  $p_{2b}$  do Cl são **INSEPARÁVEIS**

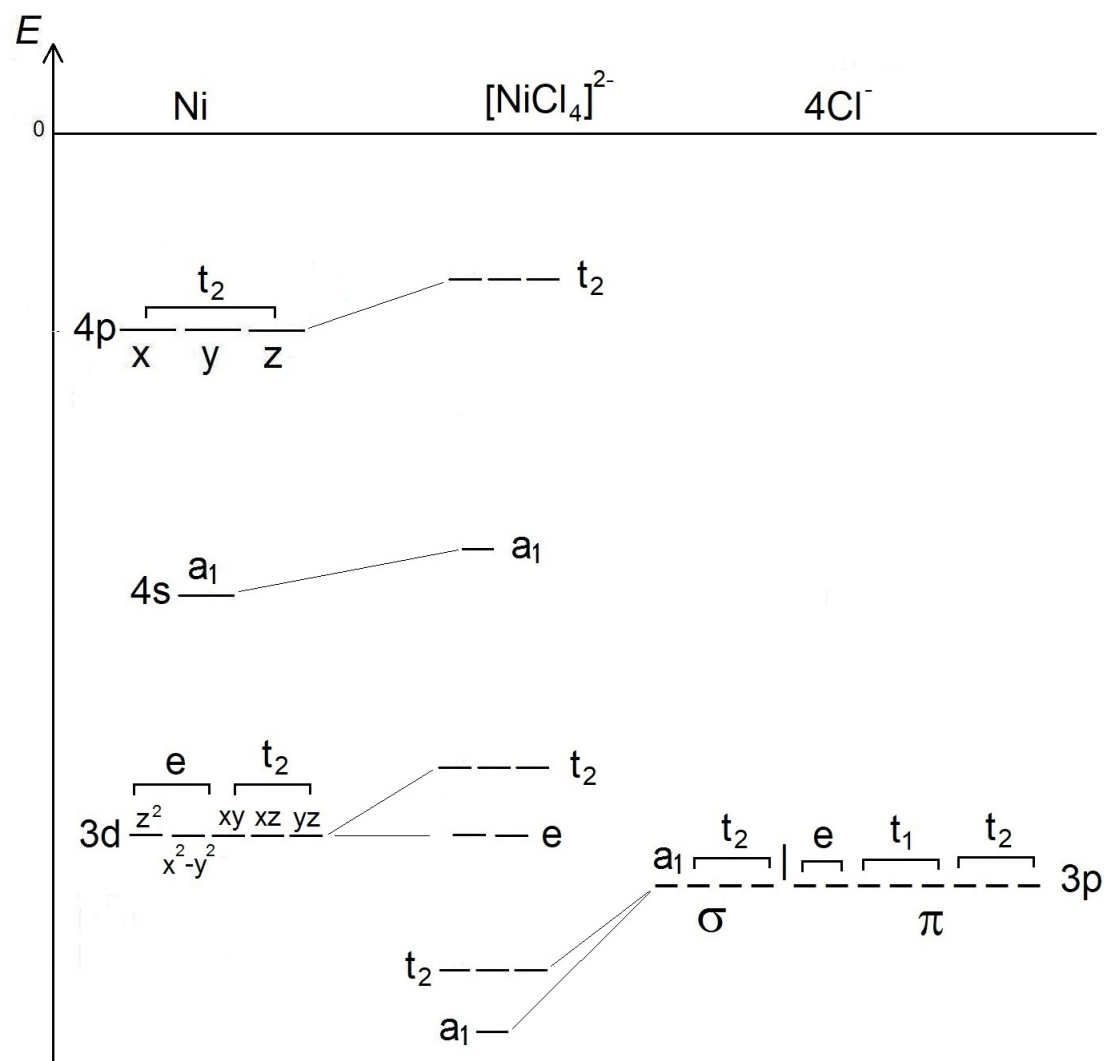
$$\begin{array}{cc}
 & \begin{array}{cc} 2p_{2a} & 2p_{2b} \end{array} \\
 \begin{array}{c} 2p_{2a} \\ 2p_{2b} \end{array} & \begin{array}{cc} 1 & 0 \\ 0 & 1 \end{array}
 \end{array}
 \xrightarrow{\text{C}_3}
 \begin{array}{cc}
 & \begin{array}{cc} 2p_{2a} & 2p_{2b} \end{array} \\
 \begin{array}{c} 2p_{2a}' \\ 2p_{2b}' \end{array} & \begin{array}{cc} -1/2 & \sqrt{3}/2 \\ -\sqrt{3}/2 & -1/2 \end{array}
 \end{array}$$

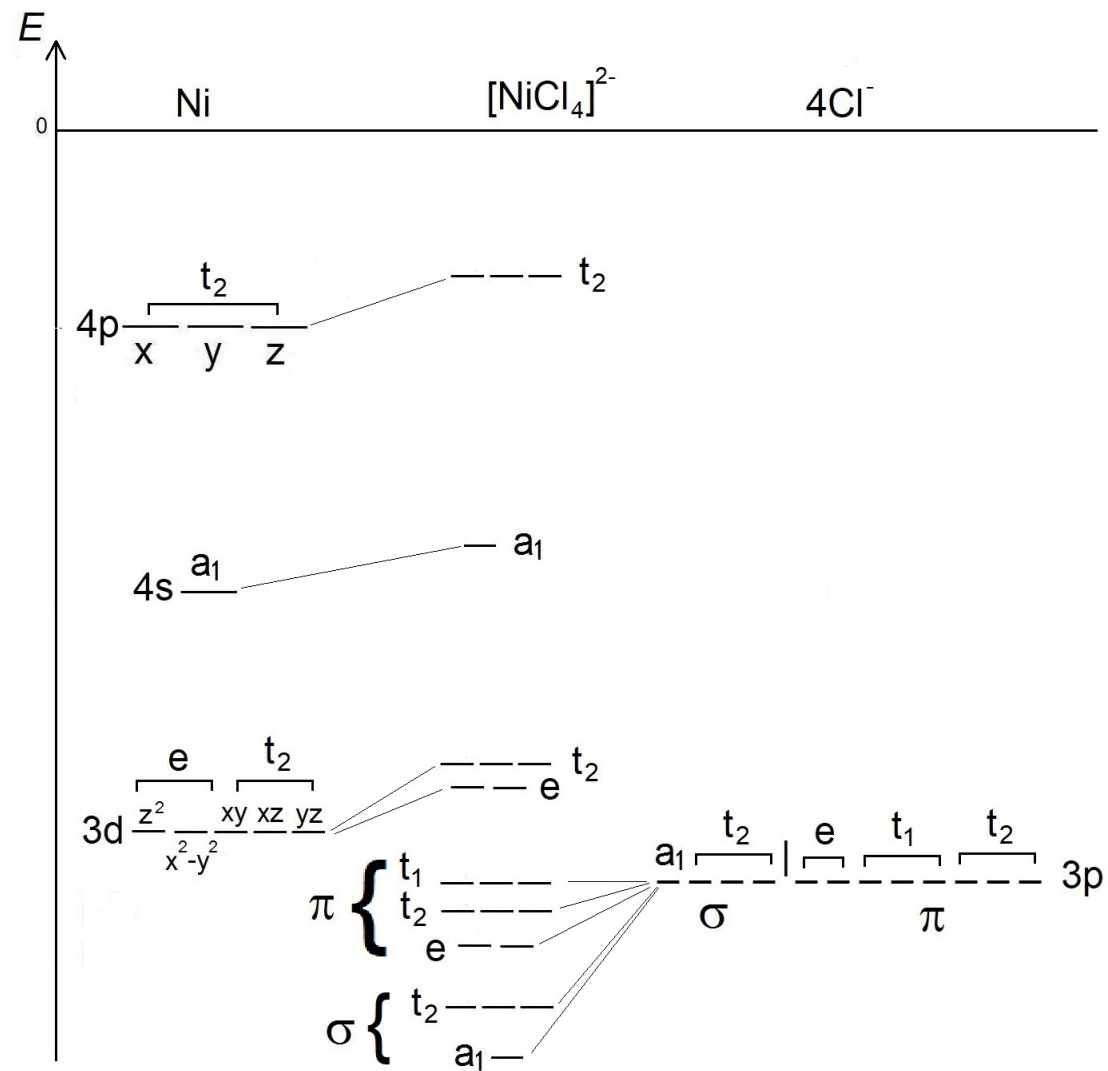
$\chi = -1$

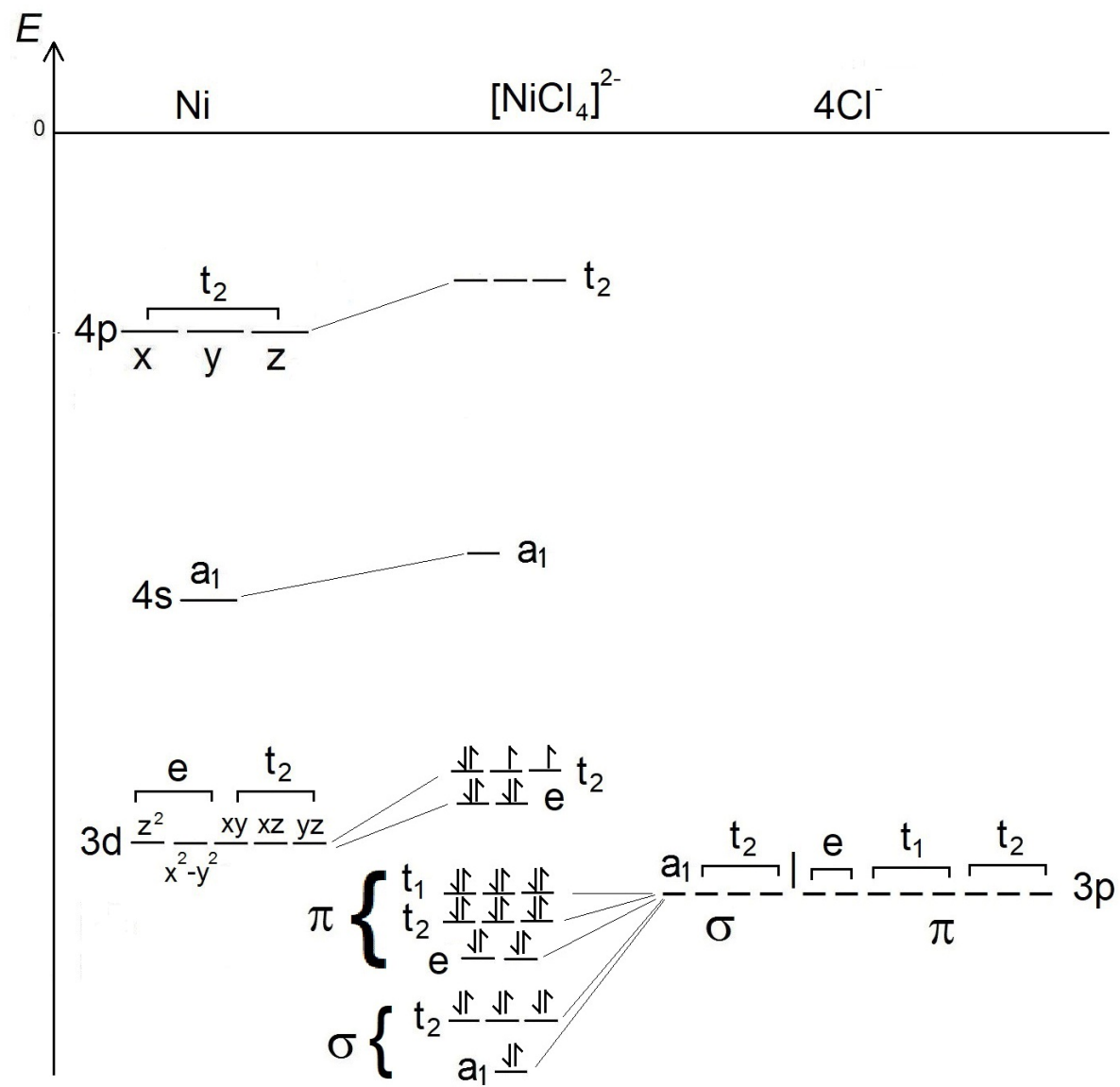
| $\text{T}_d$ | E | $8\text{C}_3$ | $3\text{C}_2$ | $6\text{S}_4$ | $6\sigma_d$ |
|--------------|---|---------------|---------------|---------------|-------------|
| $\text{A}_1$ | 1 | 1             | 1             | 1             | 1           |
| $\text{A}_2$ | 1 | 1             | 1             | -1            | -1          |
| E            | 2 | -1            | 2             | 0             | 0           |
| $\text{T}_1$ | 3 | 0             | -1            | 1             | -1          |
| $\text{T}_2$ | 3 | 0             | -1            | -1            | 1           |

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$$\begin{array}{cccccc}
 p\pi(1 \text{ a } 8) & 8 & -1 & 0 & 0 & 0
 \end{array}
 \quad \text{E} + \text{T}_1 + \text{T}_2$$

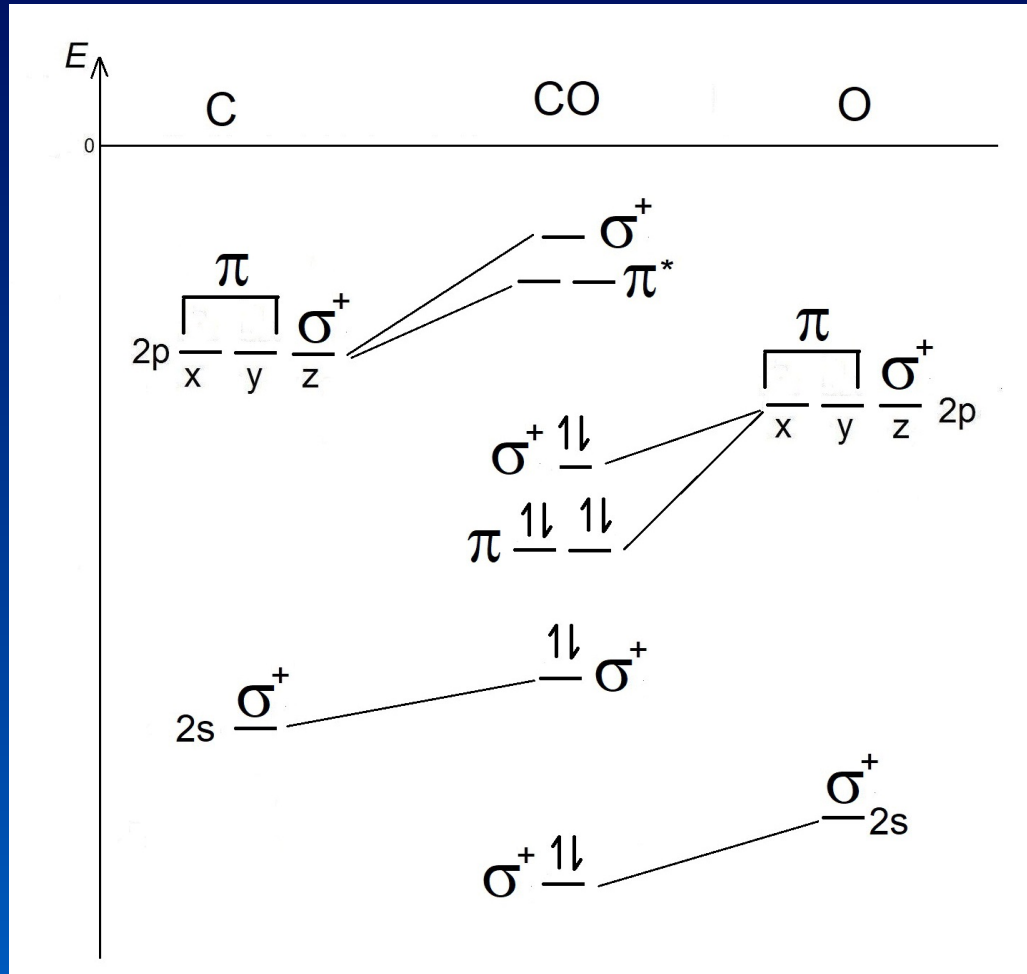






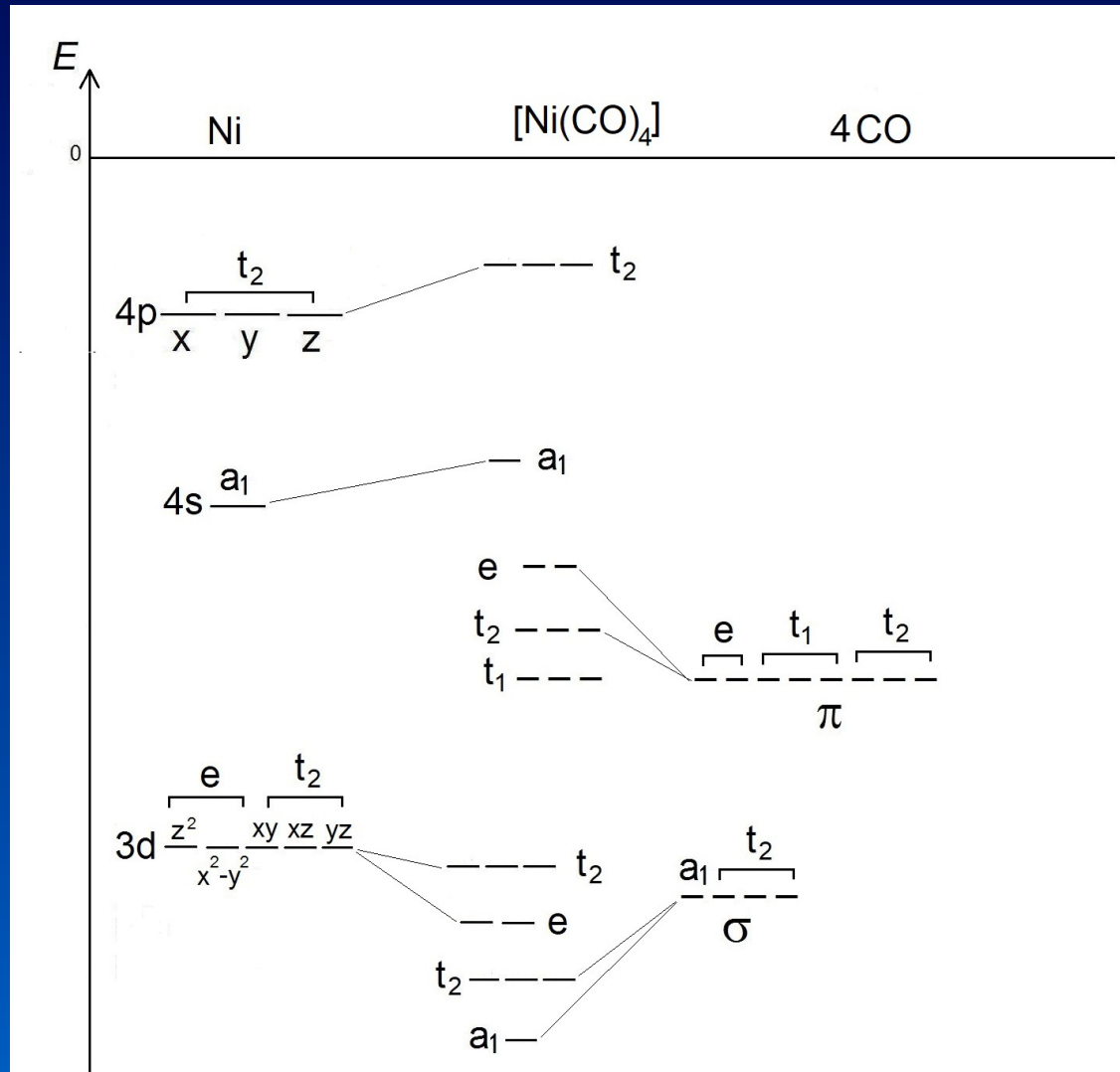
# $[\text{Ni}(\text{CO})_4] - T_d$

Diagrama de energia dos orbitais moleculares do CO



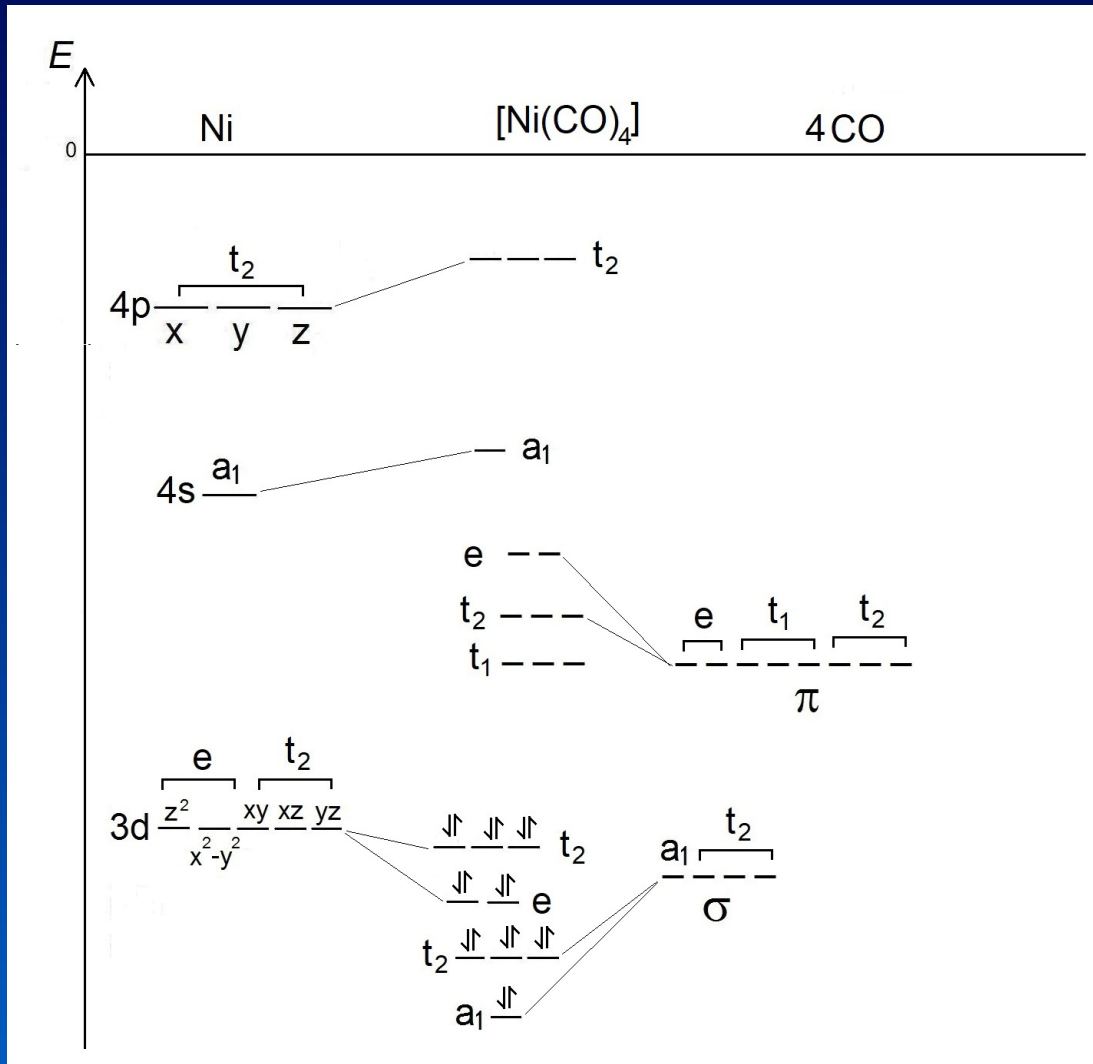


# $[\text{Ni}(\text{CO})_4] - T_d$



Aproveitando os resultados do  $[\text{NiCl}_4]^{2-} T_d$

# $[\text{Ni}(\text{CO})_4] - T_d$



18 électrons

FIM